# On the Location and Disorder of the Tetrapropylammonium (TPA) Ion in Zeolite ZSM-5 with Improved Framework Accuracy 

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#### Abstract

$\mathrm{Si}_{11.96} \mathrm{Al}_{0.04} \mathrm{O}_{24} \cdot \frac{1}{2} \mathrm{NC}_{12} \mathrm{H}_{28} \mathrm{OH}+n \mathrm{H}_{2} \mathrm{O} \quad\left(+0.04 \mathrm{Na}^{+}\right.$?), $M_{r}=822.65+(n \times 18)$, orthorhombic, Pnma (assumed), $\quad a=20.022(2), \quad b=19.899(2), \quad c=$ $13.383(1) \AA, \quad V=5332(4) \AA^{3}, \quad Z=8, \quad D_{x}=2.06$ (including TPAOH), $D_{x}=1.80 \mathrm{~g} \mathrm{~cm}^{-3}$ (for the anhydrous framework), $\lambda($ Mo $K \alpha)=0.71069 \AA, \quad \mu=$ $6.91 \mathrm{~cm}^{-1}, F(000)=3343 \cdot 7, T=293 \mathrm{~K}, R=0.042$ for 4523 observed reflections with $I>2 \cdot 0 \sigma(I)$. The framework topology agrees with earlier descriptions. Straight channels and sinusoidal channels run parallel to [010] and [100], respectively. The symmetry of the framework atoms is too close to Pnma to permit refinement in $\mathrm{Pn}_{2} a$. In the straight channel an approximate mirror plane through N and the channel axis, perpendicular to the crystallographic mirror plane, exists. The tetrapropylammonium ion lies at the intersection of the straight and sinusoidal channels in two different orientations. The two orientations, populated in a ratio of $3: 2$, are nearly related by the approximate mirror plane. Contrary to literature data the propyl-N-propyl fragments pointing into the sinusoidal and straight channel, respectively, both have CNCC torsion angles around $60^{\circ}$. No evidence is obtained for the tetrapropylammonium ion breaking the $m$ symmetry and extra disorder around $m$ is assumed. The mean $\mathrm{C}-\mathrm{C}$ and $\mathrm{C}-\mathrm{N}$ distances and mean $\mathrm{CCC}, \mathrm{CCN}$ and CNC angles, averaged over both ions, are 1.55 and $1.57 \AA$ and 109,113 and $109^{\circ}$, respectively. Contact distances smaller than $4 \cdot 0 \AA$, between terminal $C$ atoms of adjacent template ions, are in the range 3.56 (7)3.75 (2) Å.


## Introduction

The catalytic and adsorption properties of the highly siliceous ZSM-5 zeolites, crystalline aluminosilicates and of silicalite, the aluminium-free end member, have received much attention (e.g. Flanigen et al., 1978; Olson, Haag \& Lago, 1980; Haag, Lago \& Weisz, 1984). Differences in physical and chemical behaviour are often discussed in terms of differences in structure and composition of the zeolites (von

Ballmoos, 1981; Auroux, Desepert, Leclercq \& Vedrine, 1983; Gilson \& Derouane, 1984). Several papers on the crystal structure of ZSM-5 have been published recently using space group Pnma (Olson, Kokotailo, Lawton \& Meier, 1981; Price, Pluth, Smith, Bennett \& Patton, 1982; Baerlocher, 1984; Lermer, Draeger, Steffen \& Unger, 1985; Chao, Lin, Wang \& Lee, 1986). The positions of the framework atoms agree well with a tetrahedral environment of oxygen around silicon. The template molecule, tetrapropylammonium ( $\mathrm{TPA}^{+}$) fluoride or bromide or hydroxide, required for growth and stabilization (Keijsper, Mackay, van den Berg, Kortbeek \& Post, 1986) of the ZSM-5 crystals and present in the crystals as synthesized, is not always located. Two papers (Price et al., 1982; Chao et al., 1986) describe the template ion at the intersection of the straight and sinusoidal channels (Fig. 1). The $\mathrm{N}\left(\mathrm{C}_{3} \mathrm{H}_{7}\right)_{2}$ part in the sinusoidal channel is in a folded conformation in the crystallographic mirror plane. The other two $\left(\mathrm{C}_{3} \mathrm{H}_{7}\right)$ groups, pointing into the straight channel, are related by $m$. Relevant torsion angles, calculated from the published coordinates, are listed in Table 3. The TPA ${ }^{+}$ion has $m$ symmetry rather than $\overline{4}$ as found in solid TPA ${ }^{+}$. Br $^{-}$(Zalkin, 1957). However, the reported refined $\mathrm{C}-\mathrm{C}$ and $\mathrm{C}-\mathrm{N}$ bond distances in $\mathrm{TPA}^{+}$vary from 0.79 to $1.88 \AA$, the bond angles are not as expected for tetrahedral C and N atoms and several temperature factors are extremely high. In addition, the $m$ symmetry of TPA ${ }^{+}$with extended propyl groups at both sides of $m$ inevitably leads to very short contacts in the straight channel between terminal C atoms in adjacent ions. And, finally, a folded conformation of the propyl-N-propyl group in $m$ (see Fig. 1a) seems very unlikely because of the inherent substantial conformational strain caused by unfavourable short $\mathrm{H} \cdots \mathrm{H}$ contacts. Two other papers (Olson et al., 1981; Lermer et al., 1985) do not report the location of TPA ${ }^{+}$. These authors describe two nonframework atoms, called Ox 1 and Ox 2 , with low occupancy. Baerlocher (1984) refined the silicalite structure, including the TPA ${ }^{+}$ion with $m$ symmetry at $y=\frac{1}{4}$, with powder data using geometric restrictions on all distances and angles. The author suggests
disorder of TPA ${ }^{+}$in $m$ at $y=\frac{1}{4}$ but does not investigate this possibility any further. The present paper reports a detailed structure analysis of the occluded template ion in ZSM-5, without any constraints on the atoms.

## Experimental

Single crystal grown according to a prr cedure described recently (Lermer et al., 1985). Molar composition reaction mixture: $\mathrm{SiO}_{2}(12 \cdot 2), \mathrm{NaAlO}_{2}(1 \cdot 0)$, NaOH (43•3), TPABr (43•5), $\mathrm{H}_{2} \mathrm{O}$ (2452). Al (and possibly Na ) content by electron microprobe analysis (EMPA). Homogeneous Al distribution. IR measurements indicate the presence of $\mathrm{H}_{2} \mathrm{O}, \mathrm{OH}$ and possibly $\mathrm{Si}-\mathrm{OH}$ groups in the channels. Preliminary TGA measurements point to almost full occupancy of $\mathrm{TPA}^{+}$at the four channel intersections. Unit-cell contents: $\quad \mathrm{Na}_{0.32} \mathrm{Si}_{95.7} \mathrm{Al}_{0.3} \mathrm{O}_{192} .4 \mathrm{TPAOH}+n \mathrm{H}_{2} \mathrm{O}$. Full details on the growth experiments, the EMPA measurements, IR and TGA data will be published elsewhere (Jansen, van Koningsveld, Schalkoord \& van Bekkum, 1987). Crystal dimensions: $230 \times 200 \times$ $150 \mu \mathrm{~m}$. CAD-4 diffractometer, graphite-monochromated Mo $K \alpha$ radiation, cell parameters from 25 reflections with $10<\theta<17^{\circ}$. Data collected to $\theta_{\max }=$ $30 \cdot 0^{\circ}(h 0 \rightarrow 28, k 0 \rightarrow 27, l 0 \rightarrow 18), \omega / 2 \theta$ scan, width $=$ $(0.85+0.35 \tan \theta)^{\circ}$, max. recording time 240 s , $\sigma_{\text {count }}(I) / I<0.02$ requested in a scan. Three reference reflections measured every 2 h of X-ray measuring time; no change in intensity observed. Lorentz and polarization corrections (none for extinction or absorption) applied. 7944 independent reflections, 4528 with $I>2 \cdot 0 \sigma(I)$. Initial positions of framework atoms taken from literature (Olson et al., 1981). All $T$ atoms ( $\mathrm{Al}, \mathrm{Si}$ ) treated as Si . Structure refined in

(a)

(b)

Fig. 1. Conformation of $\mathrm{TPA}^{+}$as reported in the literature. (a) Folded propyl-N-propyl fragment: $\mathrm{C}\left(\alpha^{\prime}\right) \mathrm{NC}(\alpha) \mathrm{C}(\beta)=0^{\circ}$. (b) Extended propyl-N-propyl fragment $\mathrm{C}\left(\alpha^{\prime}\right) \mathrm{NC}(\alpha) \mathrm{C}(\beta)$ between 97 and $127^{\circ}$.

Pnma by (blocked) full-matrix least squares on $F$; all non-C atoms with anisotropic thermal parameters. N and C atoms located from several difference Fourier maps. H atoms not located. Attempts to locate $\mathrm{OH}^{-}$, required for electroneutrality, and $\mathrm{Na}^{+}$failed. Disordered model converged with 4523 observations [ $I>2 \cdot 0 \sigma(I)$; five low-order reflections, possibly affected by extinction, left out] to $R=0.042, w R=$ $0.044, w=1, S=0.48$, 410 parameters; $\Delta / \sigma<0.14$ for $\mathrm{Si}, \mathrm{O}$ and N and $<0 \cdot 40$ for C . ${ }^{*}$ Final $\Delta F$ synthesis has six peaks above $0.50 \mathrm{e} \AA^{-3}$ near $\mathrm{C}(5)\left(0.65 \mathrm{e} \AA^{-3}\right)$, $\mathrm{O}(14) \quad\left(0.61 \mathrm{e} \AA^{-3}\right), \quad \mathrm{C}(10) \quad\left(0.58 \mathrm{e} \AA^{-3}\right), \quad \mathrm{O}(11)$ $\left(0.56 \mathrm{e} \AA^{-3}\right)$ and $\mathrm{O}(5)\left(0.55 \mathrm{e}^{-3} \AA^{-3}\right.$. No residual density around Si atoms observed. Twenty peaks (between 0.41 and $0.49 \mathrm{e} \AA^{-3}$ ) can all be attributed to O atoms of the framework. A refinement of the framework atoms using space group $\mathrm{Pn} 2_{1} a$ failed. Apparently the deviation of the framework symmetry from Pnma is too small to permit refinement in the lower-symmetry space group $\mathrm{Pn}_{2} a$. Refinement of $\mathrm{TPA}^{+}$in $\mathrm{Pn}_{1} a$ (with fixed framework atoms in Pnma) results in a difference Fourier map containing the mirror image of TPA ${ }^{+}$. Apparently, the influence of the $\mathrm{TPA}^{+}$ion on the intensity distribution is too small to break the Pnma symmetry, or disorder around $m$ really exists. Disorder around $m$ is assumed by refining the whole structure in Pnma. All calculations performed with XRAY72 (Stewart, Kruger, Ammon, Dickinson \& Hall, 1972); atomic scattering factors of zero-valent $\mathrm{Si}, \mathrm{O}, \mathrm{N}$ and C from Cromer \& Mann (1968).

## Discussion

The final positional and isotropic thermal parameters of the framework and the template are given in Tables 1 and $2, \dagger$ respectively. A comparison with the structural data published by several authors on the same kind of structures is given in Table 3, together with some experimental details.

## The framework

The geometry of the framework is the same in all structures. The accuracy of the framework distances

[^0]Table 1. Fractional coordinates $\left(\times 10^{4}\right)$ and $U_{e q}$ values $\left(\AA^{2} \times 10^{3}\right)$ for the framework atoms

$$
U_{\mathrm{eq}}=\frac{1}{3}\left(U_{11}+U_{22}+U_{33}\right)
$$

|  | $x$ | $y$ | $z$ | $U_{\text {eq }}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Si}(1)$ | $4223 \cdot 8$ (5) | 565.0 (6) | -3359•8(9) | $17 \cdot 6$ (3) |
| $\mathrm{Si}(2)$ | 3071.6 (6) | 277.2(6) | -1893.0 (9) | 20.7 (3) |
| Si(3) | 2791.1 (6) | 612.7(6) | 312.0(9) | 19.3 (3) |
| Si(4) | 1221.5 (6) | 629.8 (6) | 267.0 (9) | 18.1 (3) |
| $\mathrm{Si}(5)$ | $712 \cdot 8$ (6) | 272-2 (6) | -1855.1 (9) | $16 \cdot 0$ (3) |
| $\mathrm{Si}(6)$ | 1864.1 (5) | $589 \cdot 6$ (6) | -3281•8 (8) | $17 \cdot 8$ (3) |
| Si(7) | $4226 \cdot 5$ (6) | -1725.0(6) | -3271.8 (9) | 18.5 (3) |
| Si(8) | 3077-8 (6) | -1301.6(6) | -1854.8 (9) | 19.9 (3) |
| $\mathrm{Si}(9)$ | 2755.4 (6) | -1727.9 (6) | $310 \cdot 9$ (9) | $17 \cdot 6$ (3) |
| Si(10) | $1205 \cdot 8$ (6) | -1731.0 (6) | 297.9 (9) | $19 \cdot 3$ (3) |
| $\mathrm{Si}(11)$ | $704 \cdot 4$ (6) | -1303.7(6) | -1820.0 (9) | 19.3 (3) |
| $\mathrm{Si}(12)$ | $1870 \cdot 6$ (6) | -1732.7(6) | -3193.3 (9) | 20.0(3) |
| $\mathrm{O}(1)$ | 3726 (2) | 534 (3) | -2442 (3) | 49 (1) |
| $\mathrm{O}(2)$ | 3084 (2) | 587 (2) | -789 (2) | 40 (1) |
| $\mathrm{O}(3)$ | 2007 (2) | 592 (3) | 289 (4) | 64 (2) |
| $\mathrm{O}(4)$ | 969 (2) | 611 (2) | -856 (3) | 44 (1) |
| $\mathrm{O}(5)$ | 1149 (2) | 541 (2) | -2763 (2) | 34 (1) |
| $\mathrm{O}(6)$ | 2435 (2) | 553 (3) | -2460 (3) | 46 (1) |
| O(7) | 3742 (2) | -1561 (2) | -2372 (3) | 47 (1) |
| $\mathrm{O}(8)$ | 3085 (2) | -1552 (2) | -728 (3) | 44 (1) |
| $\mathrm{O}(9)$ | 1980 (2) | -1554 (2) | 288 (3) | 40 (1) |
| $\mathrm{O}(10)$ | 910 (2) | -1614 (2) | -777 (3) | 58 (2) |
| $\mathrm{O}(11)$ | 1169 (2) | -1578 (2) | -2694 (3) | 48 (1) |
| $\mathrm{O}(12)$ | 2448 (2) | -1594 (3) | -2422 (3) | 55 (2) |
| $\mathrm{O}(13)$ | 3047 (3) | -510 (2) | -1866 (4) | 71 (2) |
| $\mathrm{O}(14)$ | 768 (2) | -519(2) | -1769 (3) | 47 (1) |
| $\mathrm{O}(15)$ | 4161 (2) | 1276 (2) | -3896 (3) | 44 (1) |
| O(16) | 4086 (2) | -17 (2) | -4136 (3) | 46 (1) |
| $\mathrm{O}(17)$ | 4020 (2) | -1314 (2) | -4239 (3) | 40 (1) |
| O (18) | 1886 (2) | 1298 (2) | -3836 (3) | 36 (1) |
| $\mathrm{O}(19)$ | 1940 (2) | 7 (2) | -4082 (3) | 45 (1) |
| $\mathrm{O}(20)$ | 1951 (2) | -1291(2) | -4190 (3) | 43 (1) |
| $\mathrm{O}(21)$ | -37(1) | 502 (2) | -2080 (2) | 33 (1) |
| $\mathrm{O}(22)$ | -40(2) | -1528 (2) | -2078 (3) | 40 (1) |
| $\mathrm{O}(23)$ | 4192 (3) | -2500 | -3540 (4) | 44 (2) |
| O (24) | 1884 (3) | -2500 | -3538 (4) | 34 (1) |
| O (25) | 2883 (3) | -2500 | 579 (4) | 33 (1) |
| O (26) | 1085 (3) | -2500 | 611 (4) | 30 (1) |

Table 2. Fractional coordinates $\left(\times 10^{3}\right), U_{\text {iso }}$ values $\left(\AA^{2} \times 10^{3}\right)$ and population parameters $(P P)$ of the atoms in the TPA ${ }^{+}$ions

|  | $x$ | $y$ | $z$ | $U_{\text {iso }}$ | $P P$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| N | $476 \cdot 2$ (5) | 250 | -109.5 (6) | 69 (4) | $1 \cdot 00$ |
| C(1) | 495 (1) | 233 (1) | -221(2) | 58 (8) | $0 \cdot 30$ (1) |
| C(2) | 568 (2) | 250 | -241 (2) | 97 (9) | 0.60 |
| C(3) | 578 (2) | 250 | -362 (2) | 98 (9) | $0 \cdot 60$ |
| C(4) | 399 (1) | 274 (1) | -100 (2) | 64 (8) | 0.30 |
| C(5) | 355 (1) | 228 (1) | -150(2) | 136 (10) | 0.30 |
| C(6) | 278 (2) | 250 | -147 (3) | 104 (10) | $0 \cdot 60$ |
| C(7) | 505 (2) | 319 (2) | -89(2) | 65 (8) | 0.30 |
| C(8) | 473 (2) | 334 (2) | 19 (3) | 83 (9) | 0.30 |
| $\mathrm{C}(9), \mathrm{C}\left(9^{\prime}\right)$ | 496 (1) | 412 (1) | 45 (2) | 88 (6) | $0 \cdot 50$ |
| $\mathrm{C}(10), \mathrm{C}\left(10^{\prime}\right)$ | 508 (1) | 199 (1) | -32(2) | 121 (9) | 0.50 |
| $\mathrm{C}(11), \mathrm{C}\left(11^{\prime}\right)$ | 490 (1) | 124 (1) | -45 (2) | 109 (7) | $0 \cdot 50$ |
| $\mathrm{C}(12), \mathrm{C}\left(12^{\prime}\right)$ | 529 (1) | 88 (1) | 33 (1) | 72 (4) | $0 \cdot 50$ |
| $\mathrm{C}\left(1^{\prime}\right)$ | 413 (2) | 229 (2) | -166 (4) | 83 (16) | 0.20 |
| $\mathrm{C}\left(2^{\prime}\right)$ | 355 (1) | 272 (1) | -150(2) | 136 (10) | 0.20 |
| C( $3^{\prime}$ ) | 285 (3) | 250 | -195 (4) | 110 (16) | 0.40 |
| $\mathrm{C}\left(4^{\prime}\right)$ | 534 (2) | 279 (2) | -185 (3) | 67 (12) | $0 \cdot 20$ |
| C(5) | 546 (2) | 225 (2) | -263 (4) | 73 (13) | $0 \cdot 20$ |
| $\mathrm{C}\left(6^{\prime}\right)$ | 601 (3) | 250 | -332(5) | 129 (21) | 0.40 |
| $\mathrm{C}\left(7^{\prime}\right)$ | 468 (2) | 315 (2) | -60 (3) | 61 (11) | 0.20 |
| $\mathrm{C}\left(8^{\prime}\right)$ | 516 (2) | 335 (2) | 20 (3) | 61 (10) | $0 \cdot 20$ |

and angles, reported in this paper, has been significantly improved (Table 3). On average, all twelve $\mathrm{SiO}_{4}$ groups agree well with the ideal tetrahedral environment of Si atoms. In each tetrahedron, the average $\mathrm{Si}-\mathrm{O}$ distance and $\mathrm{O}-\mathrm{Si}-\mathrm{O}$ angle are $1.587 \AA$ and $109 \cdot 47^{\circ}$, respectively, without any significant scatter. ZSM-5 has a three-dimensional channel system defined by ten-membered rings [of $T(=\mathrm{Si}, \mathrm{Al})$ atoms]. There are straight channels parallel to [010] and sinusoidal channels along [100] (see Fig. 2). The

Table 3. Comparison between several ZSM-5-like structures

| Reference | (a) | (b) | (c) | (d) | (e) | This work |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Crystal data |  |  |  |  |  |  |
| Dimensions ( $\mu \mathrm{m}$ ) | $20 \times 30 \times 40$ | $180 \times 50 \times 50$ | Powder | $260 \times 130 \times 120$ | $200 \times 70 \times 50$ | $230 \times 200 \times 150$ |
| Al/unit cell | 1.1 | 0.0 | 0.0 | 8.0 | 3.7 | 0.3 |
| Reffections with $I \geq 2 \sigma(I)$ | 1026* | 1645 | 2246 | 2217 | 1508 | 4528 |
| $\theta_{\text {max }}\left({ }^{\circ}\right)$ | Not given | 27.5 | 45.0 | 32.5 | 25.0 | 30.0 |
| $\boldsymbol{R}$ max ${ }^{\text {m }}$ | 11.9 | 6.7 | 6.9 | 9.7 | 7.9 | $4 \cdot 2$ |
| Framework geometry |  |  |  |  |  |  |
| $T$-O range ( $\AA$ ) | 1.50(4)-1.67 (3) | 1.51 (3)-1.69 (3) | 1.55-1.65 $\dagger$ | 1.54 (2)-1.62 (2) | 1.52(2)-1.66(2) | 1.567(4)-1.605 (4) |
| $\mathrm{O}-\mathrm{T}$-O range ( ${ }^{\circ}$ ) | 96 (2)-129(2) | 100 (2)-119 (2) | 104-113 | 105.6(7)-113.7 (8) | 103.9 (8)-115.5 (8) | 106.0 (2)-112.0 (2) |
| Av. $T$-O/tetrahedron (A) | 1.56-1.63 | 1.57-1.61 | 1.57-1.62 | 1.57-1.60 | 1.57-1.62 | 1.584-1.591 |
| Av. O-T-O/tetrahedron ( ${ }^{\circ}$ ) | 109-110 | 109-110 | 109.5 | 109.4-109.5 | 109-4-109-5 $\ddagger$ | 109.5 |
| TPA ${ }^{+}$-ion geometry |  |  |  |  |  |  |
| $\mathrm{C}-\mathrm{N}$ range ( $\AA$ ) | TPA not | 1.5(1)-1.9(1) | 1.54-1.55 $\dagger$ | TPA not | 1.5(1)-1.9 (1) | 1.46(3)-1.64(4) |
| $\mathrm{C}-\mathrm{C}$ range ( $\AA$ ) | localized§ | 0.8 (2)-1.8(2) | 1.51-1.55 | localized§ | 1.0(1)-1.7(1) | 1.45 (4)-1.65 (4) |
| CNC range ( ${ }^{\circ}$ ) |  | 73 (12)-140(12) | 106-112 |  | 102 (4)-116(4) | 93 (2)-122(2) |
| CCN range ( ${ }^{\circ}$ ) |  | 140(12)-179(12) | 108-113 |  | 104 (8)-160 (6) | 100 (2)-119 (3) |
| CCC range ( ${ }^{\circ}$ ) |  | 134 (12)-174 (12) | 109-112 |  | 111 (8)-144 (7) | 104 (3)-119 (3) |
| $\mathrm{C}\left(\alpha^{\prime}\right) \mathrm{NC}(\alpha) \mathrm{C}(\beta)$ torsions ( ${ }^{\circ}$ ): |  |  |  |  |  |  |
| CNCC (straight channel) |  | 124 (15) | 127 |  | 97 (8) | $67(2), 31(2) 8$ |
| CNCC (sinusoidal channel) |  | 0 | 0 |  | 0 | 51 (2), 55 (2) 1 |
| C-C** (straight channel) |  | 2.7 (2) | $3 \cdot 16$ |  | $3 \cdot 6$ (2) | $\geq 3.67$ (3) |
| C-C** (sinusoidal channel) |  | $3 \cdot 1$ (2) | $4 \cdot 46$ |  | $3 \cdot 6$ (2) | $\geq 3.56$ (7) |

References: (a) TPAOH-ZSM-5 (Olson et al., 1981); (b) TPAF-silicalite (Price et al., 1982); (c) TPAOH-silicalite (Baerlocher, 1984); (d) TPAOH-ZSM-5 (Lermer et al., 1985); (e) TPAOH-ZSM-5 (Chao et al., 1986).

[^1]Table 4. Bond lengths $(\AA)$ and bond angles $\left({ }^{\circ}\right)$ in the two TPA ${ }^{+}$ions in ZSM-5

|  | $\left(\mathrm{TPA}^{+}\right)$ | $\left(\mathrm{TPA}^{+}\right)^{\prime}$ |  | $\left(\mathrm{TPA}^{+}\right)$ | $\left(\mathrm{TPA}^{+}\right)^{\prime}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{N}-\mathrm{C}(1)$ | $1.57(2)$ | $1.53(5)$ | $\mathrm{C}(1) \mathrm{NC}(4)$ | $111(1)$ | $112(2)$ |
| $\mathrm{N}-\mathrm{C}(4)$ | $1.62(3)$ | $1.64(4)$ | $\mathrm{C}(1) \mathrm{NC}(7)$ | $106(1)$ | $111(2)$ |
| $\mathrm{N}-\mathrm{C}(7)$ | $1.52(3)$ | $1.46(4)$ | $\mathrm{C}(1) \mathrm{NC}(10)$ | $113(1)$ | $119(2)$ |
| $\mathrm{N}-\mathrm{C}(10)$ | $1.59(3)$ | $1.59(3)$ | $\mathrm{C}(4) \mathrm{NC}(7)$ | $94(1)$ | $93(2)$ |
| Mean | 1.58 | 1.56 | $\mathrm{C}(4) \mathrm{NC}(10)$ | $122(2)$ | $112(2)$ |
|  |  |  | $\mathrm{C}(7) \mathrm{NC}(10)$ | $108(2)$ | $111(2)$ |
| $\mathrm{C}(1)-\mathrm{C}(2)$ | $1.53(4)$ | $1.46(5)$ | Mean | 109 | 110 |
| $\mathrm{C}(2)-\mathrm{C}(3)$ | $1.63(5)$ | $1.58(6)$ |  |  |  |
| $\mathrm{C}(4)-\mathrm{C}(5)$ | $1.45(4)$ | $1.52(6)$ | $\mathrm{NC}(1) \mathrm{C}(2)$ | $111(2)$ | $116(3)$ |
| $\mathrm{C}(5)-\mathrm{C}(6)$ | $1.59(4)$ | $1.52(7)$ | $\mathrm{NCC(4)C(5)}$ | $111(2)$ | $107(3)$ |
| $\mathrm{C}(7)-\mathrm{C}(8)$ | $1.61(5)$ | $1.50(6)$ | $\mathrm{NC}(7) \mathrm{C}(8)$ | $100(2)$ | $119(3)$ |
| $\mathrm{C}(8)-\mathrm{C}(9)$ | $1.65(4)$ | $1.62(5)$ | $\mathrm{NC}(10) \mathrm{C}(11)$ | $117(2)$ | $117(2)$ |
| $\mathrm{C}(10)-\mathrm{C}(11)$ | $1.53(4)$ | $1.53(4)$ | Mean | 110 | 115 |
| $\mathrm{C}(1)-\mathrm{C}(12)$ | $1.48(3)$ | $1.48(3)$ |  |  |  |
| Mean | 1.56 | 1.53 | $\mathrm{C}(1) \mathrm{C}(2) \mathrm{C}(3)$ | $107(2)$ | $119(3)$ |
|  |  |  | $\mathrm{C}(4) \mathrm{C}(5) \mathrm{C}(6)$ | $114(2)$ | $107(3)$ |
|  |  |  | $\mathrm{C}(7) \mathrm{C}(8) \mathrm{C}(9)$ | $105(2)$ | $104(3)$ |
|  |  |  | $\mathrm{C}(10) \mathrm{C}(11) \mathrm{C}(12)$ | $106(2)$ | $106(3)$ |
|  |  |  | Mean | 108 | 109 |

straight channel locally has an approximate mirror plane through the channel axis, $\mathrm{Si}(1)$ and $\mathrm{Si}(7)$. The pseudo mirror plane contains N as illustrated in Fig. $3(a)$ and might explain the observed disorder of $\mathrm{TPA}^{+}$. The Si-atom numbering is given in Figs. 3(a) and $4(a)$ together with the numbering of some 0 atoms involved in short framework-to-TPA ${ }^{+}$contacts (see Table 5). The thermal vibration of the Si atoms* is essentially isotropic. The O atoms, however, have very anisotropic thermal parameters (see Figs. 3 and 4). These results might indicate a deviation of the $O$ atoms from the assumed Pnma symmetry. The deviation, however, is too small to allow refinement in the lower-symmetry space group $P n 2_{1} a$ (see Experimental).

$$
{ }^{*} \text { See deposition footnote. }
$$



Fig. 2. View of the framework along b. $T$ atoms are at the intersections of lines. $O$ atoms (not drawn) are about midway between $T$ atoms. Ten-membered rings of $T$ atoms in the straight channels are clearly visible. Some ten-membered rings, taking part in the sinusoidal channel, are hatched. Location of TPA ${ }^{+}$ions in the channels indicated by the $y$ coordinate of N atoms.

Table 5. Framework-to-TPA ${ }^{+}$distances less than $3.81 \AA$

| $\mathrm{C}(1)-\mathrm{O}(15)$ | 3.47 (2) | $\mathrm{C}(11)-\mathrm{O}(5)$ | 3.74 (2) |
| :---: | :---: | :---: | :---: |
| $\mathrm{O}(21)$ | $3 \cdot 77$ (2) | $\mathrm{O}(21)$ | 3.63 (3) |
| $\mathrm{O}(26)$ | $3 \cdot 60$ (2) | $\mathrm{C}(12)-\mathrm{O}(7)$ | 3.63 (2) |
| $\mathrm{C}(2)-\mathrm{O}(18)$ | $3 \cdot 78$ (3) | O (8) | 3.57 (2) |
| $\mathrm{O}(25)$ | 3.78 (3) | $\mathrm{O}(22)$ | 3.74 (2) |
| $\mathrm{C}(3)-\mathrm{O}(17)$ | 3.73 (3) | $\mathrm{C}\left(1^{\prime}\right)-\mathrm{O}(1)$ | 3.74 (4) |
| O(23) | $3 \cdot 80$ (3) | $\mathrm{O}(15)$ | $3 \cdot 62$ (5) |
| $\mathrm{C}(4)-\mathrm{O}(2)$ | 3.80 (2) | $\mathrm{O}(26)$ | 3.70 (5) |
| $\mathrm{O}(20)$ | $3 \cdot 63$ (3) | $\mathrm{C}\left(2^{\prime}\right)-\mathrm{O}(1)$ | 3.71 (3) |
| O(24) | 3.77 (3) | O (2) | 3.62 (3) |
| $\mathrm{C}(5)-\mathrm{O}(1)$ | 3.71 (3) | $\mathrm{O}(20)$ | $3 \cdot 80$ (3) |
| $\mathrm{O}(2)$ | $3 \cdot 62$ (3) | $\mathrm{C}\left(3^{\prime}\right)-\mathrm{O}(25)$ | 3.62 (5) |
| $\mathrm{O}(20)$ | 3.80 (3) | $\mathrm{C}\left(4^{\prime}\right)-\mathrm{O}(5)$ | 3.74 (4) |
| $\mathrm{C}(7)-\mathrm{O}(5)$ | $3 \cdot 80$ (3) | $\mathrm{O}(18)$ | 3.70 (4) |
| O(21) | 3.76 (3) | O(21) | $3 \cdot 77$ (4) |
| $\mathrm{C}(8)-\mathrm{O}(11)$ | 3.37 (4) | $\mathrm{C}\left(5^{\prime}\right)-\mathrm{O}(5)$ | 3.70 (5) |
| $\mathrm{O}(20)$ | 3.55(4) | $\mathrm{O}(15)$ | 3.66 (5) |
| $\mathrm{O}(22)$ | 3.72 (4) | $\mathrm{O}(21)$ | 3.63 (5) |
| $\mathrm{C}(9)-\mathrm{O}(11)$ | $3 \cdot 64$ (3) | $\mathrm{C}\left(8^{\prime}\right)-\mathrm{O}(7)$ | 3.65(4) |
| $\mathrm{O}(22)$ | $3 \cdot 56$ (3) | $\mathrm{O}(8)$ | 3.59 (4) |
|  |  | $\mathrm{O}(22)$ | 3.66 (4) |

## The TPA ${ }^{+}$ion

The TPA ${ }^{+}$ion is located at the intersection of the straight and sinusoidal channels in two different orientations populated in a ratio of $3: 2$. The two orientations are nearly related by the approximate mirror plane in the straight channel. Bond lengths and bond angles in the two $\mathrm{TPA}^{+}$ions are listed in Table 4. Relevant data are summarized in Table 3. The atom numbering used is depicted in Figs. 3 and 4. Contrary to recently published results (see Table 3) the TPA ${ }^{+}$ion does not lie exactly in the crystallographic mirror plane. Probably, atom $\mathrm{C}(4)$, in both $\mathrm{TPA}^{+}$ions, is refined too far from $m$ at $y=\frac{1}{4}$. If the refinement had allowed $C(4)$ to be closer to $m$, the angle $\mathrm{C}(4) \mathrm{NC}(7)$ would have opened, the angle $\mathrm{C}(4) \mathrm{NC}(10)$ would have closed and the distance $\mathrm{N}-$ $\mathrm{C}(4)$ would have become smaller, thus giving values closer to the averaged ones ( $109^{\circ}$ and $1.57 \AA$ ). The relatively large $U$ values of $\mathrm{C}(5), \mathrm{C}(10)$ and $\mathrm{C}\left(6^{\prime}\right)$ (where the prime indicates atoms in the second TPA ${ }^{+}$ ion) reflect the possibility that $\mathrm{C}(5)$ and $\mathrm{C}(10)$ do not exactly coincide with $\mathrm{C}\left(2^{\prime}\right)$ (repeated via $m$ ) and $\mathrm{C}\left(10^{\prime}\right)$ and that $\mathrm{C}\left(6^{\prime}\right)$ is not exactly in $m$ at $y=\frac{1}{4}$. A split-atom model for $C(5)\left[C(5)\right.$ and $\left.C\left(2^{\prime}\right)\right]$, gives larger $C(4)-C(5)$ and $C\left(1^{\prime}\right)-C\left(2^{\prime}\right)$ distances and smaller $C(4) C(5) C(6)$ and $C\left(1^{\prime}\right) C\left(2^{\prime}\right) C\left(3^{\prime}\right)$ angles, but does not converge satisfactorily.

The propyl-N-propyl fragments pointing into the sinusoidal and straight channels (Figs. 3 and 4) are both in a non-extended conformation. The relevant CNCC torsion angles are given in Table 3. The observed conformation of the propyl-N-propyl fragment in the sinusoidal channel has considerably less conformational strain ( $\mathrm{CNCC} \simeq 60^{\circ}$ ) than the reported folded conformation ( $\mathrm{CNCC}=0^{\circ}$ ). Therefore, the $m$ symmetry of TPA ${ }^{+}$, found by Price et al. (1982), Baerlocher (1984) and Chao et al. (1986), does not really exist. The observed conformation of TPA ${ }^{+}$in

ZSM-5 is completely different from the fully extended conformation of $\mathrm{TPA}^{+}$(symmetry $\overline{4}$ ) in solid TPA ${ }^{+} . \mathrm{Br}^{-}$(Zalkin, 1957). The $\mathrm{C}-\mathrm{C}$ contacts between terminal C atoms in neighbouring $\mathrm{TPA}^{+}$ions in the straight channel and in the sinusoidal channel are summarized in Table 3. In the present structure disorder is observed and there are three CC contacts in the straight channel: $\mathrm{C}(9)-\mathrm{C}(12) 3.67$ (3) $\mathrm{C}(9)-\mathrm{C}\left(9^{\prime}\right)$ $3 \cdot 70$ (4) and $C(12)-C\left(12^{\prime}\right) 3 \cdot 75$ (2) $\AA$. Because of the actual conformation and the tilting of the TPA ${ }^{+}$ion with respect to $m$ the contact distances are close to the expected van der Waals distances and are not as short as given in Table 3 for (b), (c) and (e). There are four CC contacts in the sinusoidal channel: $\mathrm{C}(6)-$ $\mathrm{C}\left(6^{\prime}\right) \quad 3 \cdot 56(7), \quad \mathrm{C}(6)-\mathrm{C}(3) \quad 4 \cdot 01(5), \quad \mathrm{C}\left(3^{\prime}\right)-\mathrm{C}(3)$ $4 \cdot 21$ (6) and $C\left(3^{\prime}\right)-C\left(6^{\prime}\right) 3 \cdot 70(8) \AA$. The shortest contacts involve $\mathrm{C}\left(6^{\prime}\right)$ at $y=0.250$, an atom with a large
temperature factor. The distances increase if $C\left(6^{\prime}\right)$ is not exactly in the mirror plane. The framework-toTPA ${ }^{+}$distances less than $3.81 \AA$ are given in Table 5 and illustrated in Figs. 3 and 4. The $\mathrm{C}-\mathrm{C}$ and $\mathrm{C}-\mathrm{O}$ contacts are different for the two TPA ${ }^{+}$ions. This might explain the population difference of the two TPA ${ }^{+}$ions.

The coordinates of the non-framework atoms $\mathrm{O} x 1$ and Ox2, found by Olson et al. (1981), correspond to those of the centre of gravity of atoms $C(3)$ and $C\left(6^{\prime}\right)$ and of atoms $C(6)$ and $C\left(3^{\prime}\right)$ in our study, respectively. The $\mathrm{O} x 1$ and $\mathrm{O} x 2$ atoms given by Lermer et al. (1985) are identical with $\mathrm{C}(6)$ [and $\mathrm{C}\left(3^{\prime}\right)$ ] and N in the present work, respectively. These observations strongly suggest that the template ion is also present in the structures studied by Olson et al. and Lermer et al.

(a)

(b)

(c)

Fig. 3. $\mathrm{TPA}^{+}$at the intersection of channels seen along b. Pseudo-m is indicated. For reasons of clarity the mirror image of TPA ${ }^{+}$ around $m$ at $y=\frac{1}{4}$ is not drawn. (a) Orientation of the first TPA ${ }^{+}$ion. (b) Orientation of the second TPA ${ }^{+}$ion. (c) Space-filling drawing (Spek, 1982) of TPA ${ }^{+}$in first orientation showing the packing in the straight channel. van der Waals radii taken from Bondi (1964).


Fig. 4. As Fig. 3, seen along $c$. The packing of terminal C atoms of TPA ${ }^{+}$in the sinusoidal pores is shown.

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# Conflicting Results for the Deformation Properties of Forsterite, $\mathbf{M g}_{2} \mathbf{S i O}_{\mathbf{4}}$ 

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#### Abstract

Deformation properties of forsterite have been deduced simultaneously from X-ray diffraction data affected by extinction in Bonn-Pittsburgh ( $B$ ), and in Groningen ( $G$ ). For the $G$ crystals, $G I$ and $G I I$, extinction is anisotropic and considerably larger than for crystal $B$. Measurements were made with Mo radiation for $B$, and with Mo and Ag radiation for GI and GII. As the Becker \& Coppens [Acta Cryst. (1974), A30, 129-147, 148-153; Acta Cryst. (1975), A31, 417-425] extinction model is not exact, the deformation properties had to be filtered from the data with refinement models. The flexible $B$ model [ $\alpha$ 's and populations for single exponential functions (SEF's) refined for $l=0-4$ ] and the more rigid $G$ model (SEF populations refined for $l=0-3$ and $\alpha$ for $l=0$; further $\alpha$ 's and $n$ 's fixed at standard values) yield different results. Refinement of $\alpha$ makes the majority of the SEF's notably diffuse, presumably due to correlation with incorrect extinction corrections. The order of the deformation potentials at the


$\mathrm{Mg}(1)$ and $\mathrm{Mg}(2)$ sites is reversed for $B$ and $G$. Maxima on the $\mathrm{Si}-\mathrm{O}$ bonds, which are polarized towards O , are smaller for $G\left(0 \cdot 20-0 \cdot 25 \mathrm{e}_{\AA^{-3}}\right.$ ) than for $B\left(0 \cdot 25-0.45\right.$ e $\left.\AA^{-3}\right)$. Although each of the two sets of deformation properties looks acceptable by itself, the present comparison shows that neither of them may be sufficiently close to the truth. The diffraction data are available on request from the Electron Density Data Bank (Professor H. Burzlaff, Institut für Angewandte Physik, Bismarckstrasse 10, D-8520 Erlangen, Federal Republic of Germany). Details of the measurements are described in the paper.

## Introduction

The present paper describes two independent attempts, in Bonn-Pittsburgh ( $B$ ) and in Groningen $(G)$, to determine the deformation properties of forsterite by X-ray diffraction. The conflicting results obtained show that incorrect conclusions can be drawn from deformation densities and potentials which, judged by themselves, seem reliable.


[^0]:    * A constraint refinement, using Waser constraints [ $\mathrm{C}-\mathrm{C}=$ $1.53(2), \quad \mathrm{C}-\mathrm{N}=1.54(2) \AA, \quad \mathrm{CCN}=\mathrm{CNC}=110(3)$ and $\mathrm{CCC}=$ $\left.110(2)^{\circ}\right]$ gave $R=4.3 \%$. These calculations were performed using SHELX 76 (Sheldrick, 1976) on the Cyber855 computer of the University of Utrecht with the kind cooperation of Dr A. L. Spek. The final coordinates and template geometry have been deposited.
    $\dagger$ Lists of structure factors, anisotropic thermal parameters, bond lengths and bond angles involving framework atoms, final coordinates and template geometry have been deposited with the British Library Document Supply Centre as Supplementary Publication No. SUP 43299 ( 38 pp .). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England.

[^1]:    ${ }^{*}$ For $F_{o} \geq 3 \sigma\left(F_{o}\right)$.
    $\dagger$ Constraint values; standard deviations doubtful, assumed by the author to be of the same order of magnitude as in (a) and (b).
    $\ddagger$ There is a misprint in the reported av. O-Si-O angle ( $107 \cdot 9^{\circ}$ ) and in the reported $x$ coordinate $\mathrm{C} C(6): 0 \cdot 1258$; the correct values are $109.5^{\circ}$ and 0.5128 .
    $\S$ Non-framework atoms $\mathrm{O} x 1$ and $\mathrm{O} x 2$ localized instead. [Coordinates of $\mathrm{O} x 2$ are different in reports $(a)$ and (d). See text.]
    I Values in both TPA ${ }^{+}$ions are listed. The torsion angles measuring the 'folding' are given: $\mathrm{C}(8) \mathrm{C}(7) \mathrm{NC}(10)$ in the straight channel and $\mathrm{C}(1) \mathrm{NC}(4) \mathrm{C}(5)$ in the sinusoidal channel.
    ${ }^{* *}$ Contact distances between terminal C atoms in adjacent TPA ${ }^{+}$ions.

